

THE GROWTH OF EMERGING ECONOMIES AND GLOBAL MACROECONOMIC STABILITY

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Abstract

During the last three decades we have witnessed unprecedented growth within emerging countries. As the relative size of these countries has increased, so did the global demand for financial assets issued by industrialized countries. The goal of this paper is to study how the increase in demand for financial assets have affected the macroeconomic stability of the world economy and, especially, of industrialized countries. To pursue this goal I develop a model where financial intermediaries play a central role in the intermediation of funds. Differently from other models proposed in the literature, I emphasize the role of banks in issuing financial liabilities rather than its lending role. The main finding is that the increase in demand for safe financial assets from emerging economies has increased the incentives of banks to take more leverage and contributed to greater financial and macroeconomic instability.

1 Introduction

During the last three decades we have witnessed unprecedented growth within emerging countries. As a result of the sustained growth, the size of these economies has increased dramatically compared to industrialized countries. The top panel of Figure 1 shows that, in PPP terms, the GDP of emerging countries at the beginning of the 1990s was 46 percent of the GDP of industrialized countries. This number has increased to 90 percent by 2011. When the GDP comparison is based on nominal exchange rates, the relative size of emerging economies has increased from 17 to 52 percent.

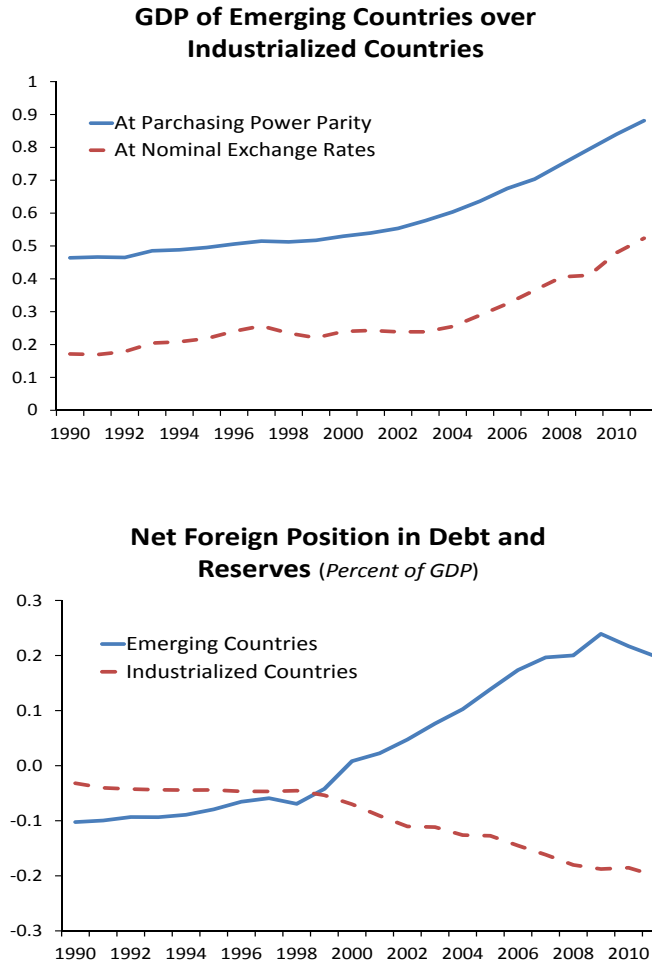


Figure 1: Gross domestic product and net foreign positions in debt instruments and international reserves of emerging and industrialized countries. **Emerging countries:** Argentina, Brazil, Bulgaria, Chile, China, Hong.Kong, Colombia, Estonia, Hungary, India, Indonesia, South Korea, Latvia, Lithuania, Malaysia, Mexico, Pakistan, Peru, Philippines, Poland, Romania, Russia, South Africa, Thailand, Turkey, Ukraine, Venezuela. **Industrialized countries:** Australia, Austria, Belgium, Canada, Denmark, Finland, France, Germany, Greece, Ireland, Italy, Japan, Netherlands, New Zealand, Norway, Portugal, Spain, Sweden, Switzerland, United.Kingdom, United.States. **Sources:** World Development Indicators (World Bank) and External Wealth of Nations Mark II database (Lane and Milesi-Ferretti (2007)).

During the same period, emerging countries have increased the foreign holdings of safe assets. It is customary to divide foreign assets in four classes:

(i) debt instruments and international reserves; (ii) portfolio investments; (iii) foreign direct investments; (iv) other investments (see Gourinchas and Rey (2007) and Lane and Milesi-Ferretti (2007)). The net foreign position in the first class of assets—debt and international reserves—is plotted in the bottom panel of Figure 1 separately for industrialized and emerging economies. Since the early 1990s, emerging countries have accumulated ‘positive’ net positions while industrialized have accumulated ‘negative’ net positions. Therefore, the increase in the relative size of emerging economies has been associated with a significant accumulation of safe financial assets by these countries.

There are several theories proposed in the literature to explain why emerging countries accumulate safe assets issued by industrialized countries. One explanation posits that emerging countries have been pursuing policies aimed at keeping their currencies undervalued and, to achieve this goal, they have been purchasing large volumes of foreign financial assets. Another explanation is based on differences in the characteristics of financial markets between emerging and industrialized countries. The idea is that lower financial development in emerging countries impairs the ability of these countries to create viable saving instruments for intertemporal smoothing (Caballero, Farhi, and Gourinchas (2008)) or for insurance purpose (Mendoza, Quadrini, and Ríos-Rull (2009)). Because of this, emerging economies turn to industrialized countries for the acquisition of these assets. A third explanation is based on greater idiosyncratic uncertainty faced by consumers and firms in emerging countries due, for example, to higher idiosyncratic risk or lower safety net provided by the public sector.

All the above explanations point to an excess demand for safe financial assets from emerging countries. As the relative size of these countries increases, so does the global demand for financial assets issued by industrialized countries. The goal of this paper is to study how this increase in demand affects the macroeconomic stability of the world economy and, in particular, of industrialized countries.

To pursue this goal, I develop a model where financial intermediaries play a central role in the intermediation of funds from agents in excess of funds (lenders) to agents in need of funds (borrowers). Financial intermediaries issue liabilities and make loans. However, differently from recent macroeconomic models studied in the literature,¹ I emphasize the central role of banks

¹See, for example, Van den Heuvel (2008), Meh and Moran (2010), Brunnermeier and Sannikov (2010), Gertler and Kiyotaki (2010), Mendoza and Quadrini (2010), De Fiore

in issuing financial liabilities (or facilitating the issuance of liabilities) rather than its lending role.

An important role played by bank liabilities is that they can be held by other sectors of the economy for insurance purposes. Then, when the supply of bank liabilities increases, agents that hold these liabilities are better insured and are willing to engage in activities that are individually risky. In aggregate, this allows for sustained employment, production and consumption. However, when banks issue more liabilities, they also create the conditions for a liquidity crisis. A crisis generates a drop in the volume of intermediated funds and with it a fall in the stock of bank liabilities held by the nonfinancial sector. As a consequence of this, the nonfinancial sector will be less willing to engage in risky activities with a consequent decline in real economic activity.

The probability and macroeconomic consequences of a liquidity crisis depend on the leverage chosen by banks, which in turn depends on the interest rate paid on their liabilities (funding cost). When the interest rate is low, banks have more incentives to leverage, which in turn increases the likelihood of a liquidity crisis. It is then easy to see how the growth of emerging countries could contribute to global economic instability. As the share of these countries in the world economy increases, the demand for assets issued by industrialized countries (bank liabilities in the model) rises. This drives down the interest rate paid by banks on their liabilities, increasing the incentives to take more leverage. But as the banking sector in industrialized countries becomes more leveraged, the likelihood of a systemic crisis starts to emerge and/or the consequences of a crisis become bigger. As long as a crisis does not materialize, the economy enjoys sustained levels of financial intermediation, asset prices and economic activity. But, eventually, the arrival of a crisis induces a reversal in financial intermediation with a fall in asset prices and overall economic activity.

The organization of the paper is as follows. Section 2 describes the model and characterizes the equilibrium. Section 3 applies the model to study how the increasing demand for financial assets from emerging economies have affected the stability of the macro-economy. Section 4 concludes.

and Uhlig (2011), Gertler and Karadi (2011), Boissay, Collard, and Smets (2010), Corbae and D'Erasmus (2012), Rampini and Viswanathan (2012), Adrian, Colla, and Shin (2013).

2 Model

There are three sectors: the entrepreneurial sector, the worker sector and the financial intermediation sector. The role of the financial intermediation sector is to facilitate the transfer of resources between entrepreneurs and workers. In the process of intermediating funds, however, financial intermediaries might have an incentive to leverage which could create the conditions for financial and macroeconomic instability.

I describe first the entrepreneurial and worker sectors. After characterizing the equilibrium with direct borrowing and lending between these two sectors, I introduce the financial intermediation sector under the assumption that direct borrowing and lending is not possible or efficient.

2.1 Entrepreneurial sector

In the entrepreneurial sector there is a unit mass of entrepreneurs, indexed by i , with lifetime utility $\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \ln(c_t^i)$. Entrepreneurs are individual owners of firms, each operating the production function $y_t^i = z_t^i h_t^i$, where h_t^i is the input of labor supplied by workers at the market wage w_t , and z_t^i is an idiosyncratic productivity shock. The productivity shock is independently and identically distributed among firms and over time, with probability distribution $\Gamma(z)$. As in Arellano, Bai, and Kehoe (2011), the input of labor h_t^i is chosen before observing z_t^i , and therefore, labor is risky.

Entrepreneurs have access to a market for non-contingent bonds with gross interest rate R_t^b . The bonds held by entrepreneurs are the liabilities issued by banks and specified later.

An entrepreneur i enters period t with bonds b_t^i and chooses the labor input h_t^i . After the realization of the idiosyncratic shock z_t^i , he/she chooses consumption c_t^i and next period bonds b_{t+1}^i . The budget constraint is

$$c_t^i + \frac{b_{t+1}^i}{R_t^b} = (z_t^i - w_t)h_t^i + b_t^i. \quad (1)$$

Because labor h_t^i is chosen before the realization of z_t^i , while the saving decision is made after the observation of z_t^i , it will be convenient to define $a_t^i = b_t^i + (z_t^i - w_t)h_t^i$ the entrepreneur's wealth after production. Given the timing structure, the input of labor h_t^i depends on b_t^i while the saving choice b_{t+1}^i depends on a_t^i . The optimal entrepreneur's policies are characterized by the following lemma:

Lemma 2.1 *Let ϕ_t satisfy the condition $\mathbb{E}_z \left\{ \frac{z-w_t}{1+(z-w_t)\phi_t} \right\} = 0$. The optimal entrepreneur's policies are*

$$\begin{aligned} h_t^i &= \phi_t b_t^i, \\ c_t^i &= (1 - \beta) a_t^i, \\ \frac{b_{t+1}^i}{R_t^b} &= \beta a_t^i. \end{aligned}$$

Proof 2.1 *See Appendix A.*

The demand for labor is linear in the initial wealth of the entrepreneur b_t^i . The term of proportionality ϕ_t is defined by condition $\mathbb{E}_z \left\{ \frac{z-w_t}{1+(z-w_t)\phi_t} \right\} = 0$, where the expectation is over the idiosyncratic shock z with probability distribution $\Gamma(z)$. Since the only endogenous variable that affects ϕ_t is the wage rate, I will denote this term by the function $\phi(w_t)$. It can be verified that this function is strictly decreasing in w_t .

Because $\phi(w_t)$ is the same for all entrepreneurs, I can derive the aggregate demand for labor as

$$H_t = \phi(w_t) \int_i b_t^i = \phi(w_t) B_t,$$

where capital letters denote average (per-capita) variables. The aggregate demand depends negatively on the wage rate—which is a standard property—and positively on the financial wealth of entrepreneurs—which is a special property of this model. This derives from the fact that labor is risky and entrepreneurs are willing to hire labor only if they hold financial wealth for consumption smoothing.

Also linear is the consumption policy which follows from the logarithmic specification of the utility function. This property allows for linear aggregation. Another property worth emphasizing is that in a stationary equilibrium with constant B_t , the interest rate must be lower than the intertemporal discount rate,² that is, $R^b < 1/\beta - 1$.

²To see this, consider the first order condition of an individual entrepreneur for the choice of b_{t+1}^i . This is the typical euler equation that, with log preferences, takes the form $1/c_t^i = \beta R^b \mathbb{E}_t(1/c_{t+1}^i)$. Because individual consumption c_{t+1}^i is stochastic, $\mathbb{E}_t(1/c_{t+1}^i) > 1/\mathbb{E}_t c_{t+1}^i$. Therefore, if $\beta R^b = 1$, we would have that $\mathbb{E}_t c_{t+1}^i > c_t^i$, implying that individual consumption would grow on average. But then aggregate consumption would not be bounded, which violates the hypothesis of a stationary equilibrium. I will come back to this property later.

2.2 Worker sector

There is a unit mass of workers with lifetime utility $\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left(c_t - \alpha \frac{h_t^{1+\frac{1}{\nu}}}{1+\frac{1}{\nu}} \right)$, where c_t is consumption and h_t is the supply of labor. Workers do not face idiosyncratic risks and the assumption of risk neutrality is not important for the key results of the paper as will be discussed later.

Each worker holds a non-reproducible asset available in fixed supply \bar{K} , with each unit producing χ units of consumption goods. The asset is divisible and can be traded at the market price p_t . We can think of the asset as housing and χ as the services produced by one unit of housing. Workers can borrow at the gross interest rate R_t^l and face the budget constraint

$$c_t + l_t + (k_{t+1} - k_t)p_t = \frac{l_{t+1}}{R_t^l} + w_t h_t + \chi k_t,$$

where l_t is the loan contracted in period $t - 1$ and due in the current period t , and l_{t+1} is the new debt that will be repaid in the next period $t + 1$.

Debt is constrained by a borrowing limit. I will consider two specifications. In the first specification the borrowing limit takes the form

$$l_{t+1} \leq \eta, \tag{2}$$

where η is constant. Later I will consider a borrowing constraint that depends on the collateral value of assets, that is,

$$l_{t+1} \leq \eta \mathbb{E}_t p_{t+1} k_{t+1}. \tag{3}$$

The borrowing constraint (2) allows me to characterize the equilibrium analytically. However, the asset price p_t is constant. With the borrowing constraint (3), instead, the model also provides interesting predictions about the asset price p_t but the full characterization of the equilibrium can be done only numerically.

Appendix C writes down the workers' problem and derives the first order conditions. When the borrowing constraint takes the form specified in (2), the optimality conditions are

$$\alpha h_t^{\frac{1}{\nu}} = w_t, \tag{4}$$

$$1 = \beta R_t^l (1 + \mu_t), \tag{5}$$

$$p_t = \beta \mathbb{E}_t (\chi + p_{t+1}), \tag{6}$$

where $\beta\mu_t$ is the Lagrange multiplier associated with the borrowing constraint. When the borrowing constraint takes the form specified in (3), only the first order condition with respect to k_{t+1} differs, taking the form

$$p_t = \beta\mathbb{E}_t\left[\chi + (1 + \eta\mu_t)p_{t+1}\right]. \quad (7)$$

2.3 Equilibrium with direct borrowing and lending

Before introducing the financial intermediation sector it would be instructive to characterize the equilibrium with direct borrowing and lending. In this case the bonds held by entrepreneurs are equal to the loans taken by workers and market clearing implies $R_t^b = R_t^l = R_t$.

Proposition 2.1 *In absence of aggregate shocks, the economy converges to a steady state in which workers borrow from entrepreneurs and $\beta R < 1$.*

Proof 2.1 *See Appendix B*

The fact that the steady state interest rate is lower than the intertemporal discount rate is a consequence of the uninsurable risk faced by entrepreneurs. If $\beta R = 1$, entrepreneurs would continue to accumulate bonds without limit in order to insure the idiosyncratic risk. The supply of bonds from workers, however, is limited by the borrowing constraint of workers. To insure that entrepreneurs do not accumulate an infinite amount of bonds, the interest rate has to fall below the intertemporal discount rate.

The equilibrium in the labor market can be characterized as the simple intersection of aggregate demand and supply as depicted in Figure 2. The aggregate demand was derived in the previous subsection and takes the form $H_t^D = \phi(w_t)B_t$. It depends negatively on the wage rate w_t and positively on the aggregate wealth (bonds) of entrepreneurs, B_t . The supply is derived from the households' first order condition (4) and takes the form $H_t^S = \left(\frac{w_t}{\alpha}\right)^\nu$.

The dependence of the demand of labor from the financial wealth of entrepreneurs is a key property of this model. When entrepreneurs hold a lower value of B_t , the demand for labor declines and in equilibrium there is lower employment and production. Importantly, the reason lower values of B_t decreases the demand of labor is not because employers do not have funds to finance hiring or because they face a higher financing cost. In fact, employers do not need any financing to hire and produce. Instead, the transmission

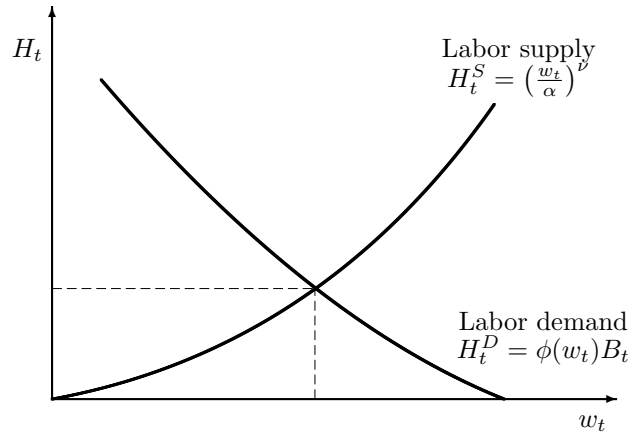


Figure 2: Labor market equilibrium.

mechanism is based on the lower financial wealth of entrepreneurs which is held as an insurance buffer against the idiosyncratic risk. This mechanism is clearly distinct from the traditional ‘credit channel’ where firms are in need of funds to finance employment (for example, because wages are paid in advance) or to finance investment.

The next step is to introduce financial intermediaries and show that a fall in B_t could be the result of a crisis that originates in the financial sector.

Discussion In the equilibrium described above, producers (entrepreneurs) are net savers while workers are net borrowers. Since it is customary to work with models in which firms are net borrowers (for example in the studies referenced in the introduction), this property may seem counterfactual. This financial structure, however, is not inconsistent with the recent changes observed in the United States.

It is well known that during the last two and half decades, US corporations have increased their holdings of financial assets. As shown in Figure 3, the *net* financial assets—that is, the difference between financial assets and liabilities—have become positive in the 2000s for the nonfinancial corporate sector. The only exception is at the pick of the 2008 crisis when the financial assets held by corporations declined in value. Therefore, recent evidence shows that US corporations are no longer net borrowers in aggregate.

The reversal from net borrower to net lender did not arise in the noncorporate sector. The net financial assets of the noncorporate sector remained

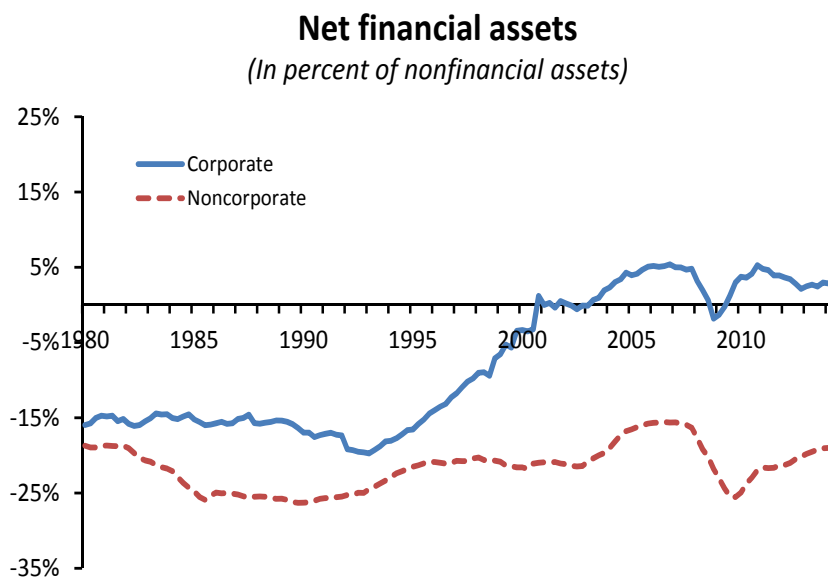


Figure 3: Net financial assets (assets minus liabilities) in the nonfinancial business sector as a percentage of nonfinancial assets. Source: Flows of Funds Accounts.

negative, without any particular upward or downward trend. Still, the change experienced by the corporate sector shows that a large segment of the business sector is no longer dependent on external financing.³ Of course, these are just aggregate numbers and, possibly, there is significant heterogeneity. However, these numbers suggest that the proportion of financially dependent firms has declined significantly over time. This pattern is shown in more details in Shourideh and Zetlin-Jones (2012) using data from the Flows of Funds and firm level data from Compustat. Also related is Eisfeldt and Muir (2012) showing that there is a strong correlation between the funds raised externally by corporations and their accumulation of liquid financial assets (suggesting that raising external funds does not necessarily increase the net financial liabilities of firms). The model developed here is meant to capture the growing importance of firms that are no longer dependent on external financing.

The second remark relates to the statement that firms are not dependent

³If we aggregate the corporate sector with the noncorporate sector, the overall net borrowing remains positive but has declined dramatically from about 20 percent in the early nineties to about 5 percent.

on external financing if they hold positive net financial assets. This definition of external dependence is purely static and captures the idea that a firm is capable of increasing spending in the current period only if it has the option of borrowing more. Similarly, a firm is financially independent if it can increase its current spending without the need of borrowing. This definition of financial independence, however, does not guarantee that a firm is financially independent in the future. Negative shocks could reduce the financial wealth of entrepreneurs and force them to cut future consumption (or dividends). Still, this is different from traditional models with financial constraints on firms. In these models, the financial mechanism affects the production and investment decisions of firms in important ways only when they are financially constrained in the period in which these decisions are made. More specifically, only when the current multiplier associated with the borrowing constraint becomes positive.

The third remark is that the equilibrium outcome of having the entrepreneurial sector to be a net lender does not derive from the assumption that entrepreneurs are more risk-averse than workers. Instead, it follows from the assumption that only entrepreneurs are exposed to uninsurable risks. As long as producers face more risk than workers, the former would continue to lend to the latter even if workers were risk averse.

The final remark relates to the assumption that the idiosyncratic risk faced by entrepreneurs cannot be insured away (market incompleteness). Given that workers are risk neutral, it would be optimal for entrepreneurs to offer a wage that is contingent on the output of the firm. Although this is excluded by assumption, it is not difficult to extend the model so that the lack of insurance from workers is an endogenous outcome of information asymmetries. The idea is that, when the wage is state-contingent, firms could use their information advantage about the performance of the firm to gain opportunistically from workers. The same argument can be used to justify more generally the absence of a market for contingent claims. Since this is well known in the literature, I decided to impose the absence of an insurance market for idiosyncratic risks by assumption.

2.4 Financial intermediation sector

If direct borrowing is not feasible or inefficient, financial intermediaries becomes important for transferring funds from lenders (entrepreneurs) to borrowers (workers) and to create financial assets that could be held for insur-

ance purposes. It is under this assumption that I introduce the financial intermediation sector.

There is a continuum of infinitely lived banks owned by workers. Even if I use the term ‘banks’ as a reference to financial intermediaries, it should be clear that the financial sector in the model is representative of all financial firms, not only traditional commercial banks. The assumption that banks are held by workers, as opposed to entrepreneurs, makes the analysis simpler because workers are risk neutral while entrepreneurs are risk averse.

Banks start the period with loans made to workers, l_t , and liabilities held by entrepreneurs, b_t . The difference between loans and liabilities is the bank equity $e_t = l_t - b_t$.

Given the beginning of period balance sheet position, the bank could default on its liabilities. In case of default creditors have the right to liquidate the bank assets l_t . However, they may not recover the full value of the assets. In particular, with probability λ creditors recover only a fraction $\underline{\xi} < 1$.

It will be convenient to define the variable $\xi_t \in \{\underline{\xi}, 1\}$ as the fraction of the bank assets recovered by creditors in the event of default. The recovery value can then be written more generally as $\xi_t l_t$. Therefore, with probability λ creditors recover $\underline{\xi} l_t$ and with probability $1 - \lambda$ they recover the full value l_t . The variable ξ_t is the same for all banks (aggregate stochastic variable) and its value is unknown when the bank issued the liabilities b_t and made the loans l_t in period $t - 1$.

The recovery fraction ξ_t will be derived endogenously in the model. For the moment, however, it will be convenient to think of ξ_t as an exogenous stochastic variable.

Once $\xi_t \in \{\underline{\xi}, 1\}$ becomes known at the beginning of period t , the bank could use the threat of default to renegotiate the outstanding liabilities. Assuming that the bank has the whole bargaining power, the liabilities can be renegotiated to $\xi_t l_t$. Therefore, after renegotiation, the residual liabilities of the bank are

$$\tilde{b}_t(b_t, l_t) = \begin{cases} b_t, & \text{if } b_t \leq \xi_t l_t \\ \xi_t l_t & \text{if } b_t > \xi_t l_t \end{cases} \quad (8)$$

Renegotiation, however, is costly for a bank. More specifically, in case of

renegotiation the bank incurs the cost

$$\tilde{\varphi}_t(b_{t+1}, l_t) = \begin{cases} 0, & \text{if } b_t \leq \xi_t l_t \\ \varphi\left(\frac{b_t - \xi_t l_t}{l_t}\right) b_t & \text{if } b_t > \xi_t l_t \end{cases}. \quad (9)$$

The function $\varphi(\cdot)$ is strictly increasing and convex, differentiable and satisfies $\varphi(0) = \varphi'(0) = 0$. Furthermore, I assume that $\varphi(1 - \underline{\xi}) < 1 - \underline{\xi}$. This property guarantees that the gain from renegotiation (which happens when $b_t > \xi_t l_t$) is always positive for the bank.⁴

The possibility of renegotiation implies potential losses for investors (entrepreneurs), which are fully internalized by the market when the bank issues the new liabilities b_{t+1} and makes the new loans l_{t+1} .

Denote by \bar{R}_t^b the expected gross return on the market portfolio of bank liabilities issued in period t and repaid in period $t + 1$ (expected return on liabilities issued by the whole banking sector). Since banks are atomistic and the sector is competitive, the expected return on the liabilities issued by an individual bank must be equal to the aggregate expected return \bar{R}_t^b . Therefore, the price of liabilities $q_t(b_{t+1}, l_{t+1})$ issued by an individual bank at t must satisfy

$$q_t(b_{t+1}, l_{t+1}) b_{t+1} = \frac{1}{\bar{R}_t^b} \mathbb{E}_t \tilde{b}_{t+1}(b_{t+1}, l_{t+1}). \quad (10)$$

The left-hand-side is the payment made by investors (entrepreneurs) for the purchase of b_{t+1} . The term on the right-hand-side is the expected repayment in the next period, discounted by \bar{R}_t^b (the expected market return).

The final assumption is that banks incur an operation cost τ per unit of raised funds. This parameter captures the efficiency of the intermediation sector. Later, in the application of the model, I will interpret changes in τ as the result of financial innovations.

⁴Banks do not borrow more than l_t because this will trigger renegotiation with probability 1. Therefore, renegotiation can only arise when $\xi_t = \underline{\xi}$. Provided that $b_t > \underline{\xi} l_t$, the debt reduction from renegotiating is $b_t - \underline{\xi} l_t$. This is a gain that is compared to the cost $\varphi(b_t/l_t - \underline{\xi}) b_t$. Suppose that $b_t = l_t$ (maximum leverage). In this case the gain from renegotiation is $l_t - \underline{\xi} l_t$ while the cost is $\varphi(1 - \underline{\xi}) b_t$. Since $b_t < l_t$, we can verify that the gain is bigger than the cost if $\varphi(1 - \underline{\xi}) < 1 - \underline{\xi}$. The concavity of $\varphi(\cdot)$ implies that this is also true when the bank chooses a leverage smaller than the maximum, that is, $b_t < l_t$.

The budget constraint of the bank, after renegotiation, can be written as

$$\tilde{b}_t(b_t, l_t) + \tilde{\varphi}_t(b_t, l_t) + \frac{l_{t+1}}{R_t^l} + d_t = l_t + (1 - \tau) \left[\frac{\mathbb{E}_t \tilde{b}_{t+1}(b_{t+1}, l_{t+1})}{\bar{R}_t^b} \right], \quad (11)$$

where d_t are the dividends paid to shareholders (workers) and the functions $\tilde{b}_t(b_t, l_t)$ and $\tilde{\varphi}_t(b_t, l_t)$ are defined in (8) and (9). The last term in the budget constraint denotes the funds raised by issuing new liabilities b_{t+1} . According to equation (10), these funds are equal to $\mathbb{E}_t \tilde{b}_{t+1}(b_{t+1}, l_{t+1}) / \bar{R}_t^b$. They are multiplied by $1 - \tau$ because of the operation cost.

The problem solved by the bank can be written recursively as

$$V_t(b_t, l_t) = \max_{d_t, b_{t+1}, l_{t+1}} \left\{ d_t + \beta \mathbb{E}_t V_{t+1}(b_{t+1}, l_{t+1}) \right\} \quad (12)$$

subject to (8), (9), (11).

The decision to renegotiate existing liabilities is implicitly accounted by the functions $\tilde{b}_t(b_t, l_t)$ and $\tilde{\varphi}_t(b_t, l_t)$. The leverage cannot exceed 1 since in this case the bank would renegotiate with certainty. Once the probability of renegotiation is 1, a further increase in b_{t+1} does not increase the borrowed funds $[(1 - \tau) / \bar{R}_t^b] \mathbb{E}_t \tilde{b}_{t+1}(b_{t+1}, l_{t+1})$ but raises the renegotiation cost. Therefore, Problem (12) is also subject to the constraint $b_{t+1} \leq l_{t+1}$.

The optimal policies of the bank are characterized by the first order conditions with respect to b_{t+1} and l_{t+1} . Denote by $\omega_{t+1} = b_{t+1} / l_{t+1}$ the bank leverage. The first order conditions, derived in Appendix D, take the form

$$\frac{1 - \tau}{\bar{R}_t^b} \geq \beta \left[1 + \frac{\theta(\omega_{t+1}) \left(\varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1} + \varphi(\omega_{t+1} - \underline{\xi}) \right)}{1 - \theta(\omega_{t+1})} \right], \quad (13)$$

$$\frac{1}{R_t^l} \geq \beta \left[1 + \theta(\omega_{t+1}) \varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1}^2 + \theta(\omega_{t+1}) \underline{\xi} \left(\frac{1 - \tau}{\beta \bar{R}_t^b} - 1 \right) \right] \quad (14)$$

where the inequality sign applies if $\omega_{t+1} = 1$. The variable $\theta(\omega_{t+1})$ is the

probability that the bank renegotiates at $t + 1$, defined as

$$\theta(\omega_{t+1}) = \begin{cases} 0, & \text{if } \omega_{t+1} < \underline{\xi} \\ \lambda, & \text{if } \underline{\xi} \leq \omega_{t+1} \leq 1 \\ 1, & \text{if } \omega_{t+1} > 1 \end{cases}$$

The first conditions make clear that it is the leverage of the firm $\omega_{t+1} = b_{t+1}/l_{t+1}$ that matters, not the scale of operation b_{t+1} or l_{t+1} . This follows from the linearity of the intermediation technology and the risk neutrality of banks. The leverage matters because the renegotiation cost is convex in the leverage. These properties imply that in equilibrium all banks choose the same leverage (although they could chose different scales of operation).

Because the first order conditions (13) and (14) depend only on one individual variable, the leverage ω_{t+1} , there is no guarantee that these conditions are both satisfied for arbitrary values of \bar{R}_t^b and R_t^l . In the general equilibrium, however, these rates adjust to clear the markets for bank liabilities and loans and both conditions will be satisfied.

Further exploration of the first order conditions reveals that, if banks choose a low leverage, that is, $\omega_{t+1} < \underline{\xi}$, then the cost of liabilities (including the operation cost) and the lending rate must be equal to the discount rate, that is, $\bar{R}_t^b/(1 - \tau) = R_t^l = 1/\beta$. However, if banks choose $\omega_{t+1} > \underline{\xi}$, the funding cost $\bar{R}_t^b/(1 - \tau)$ must be smaller than the interest rate on loans. This is necessary to cover the renegotiation cost incurred with probability λ .

Lemma 2.2 *If the leverage is $\omega_{t+1} \leq \underline{\xi}$, then $\frac{\bar{R}_t^b}{1-\tau} = R_t^l = \frac{1}{\beta}$. If the leverage is $\omega_{t+1} > \underline{\xi}$, then $\frac{\bar{R}_t^b}{1-\tau} < R_t^l < \frac{1}{\beta}$.*

Proof 2.2 *See Appendix E*

Therefore, once the leverage of banks exceeds $\underline{\xi}$, there is a spread between the funding rate (inclusive of the operation cost τ) and the lending rate. Intuitively, raising the leverage ω_{t+1} above $\underline{\xi}$ increases the expected renegotiation cost. The bank will choose to do so only if there is a spread between the cost of funds and the return on the investment. As the spread increases so does the leverage chosen by banks. As we will see, the spread

increases when there is more demand for banks liabilities (for example from emerging countries) or the operation cost τ declines (due, for example, to financial innovations). As the leverage increases above $\underline{\xi}$, banks could default with positive probability. This generates a loss of financial wealth for entrepreneurs, causing a macroeconomic contraction through the ‘bank liabilities channel’ as described earlier.

2.5 Banking liquidity and endogenous ξ_t

To make ξ_t endogenous, I now interpret this variable as the liquidation price of bank assets. This price will be determined in equilibrium and the liquidity of the whole banking sector plays a central role in determining this price.

Assumption 1 *If a bank is liquidated, the assets l_t are divisible and can be sold either to other banks or to other sectors (workers and entrepreneurs). However, other sector can recover only a fraction $\underline{\xi} < 1$.*

Therefore, in the event of liquidation, it is more efficient to sell the liquidated assets to other banks since they have the ability to recover the whole asset value l_t while other sectors can recover only $\underline{\xi}l_t$. This is a natural assumption since banks have, supposedly, a comparative advantage in the management of financial investments. However, even if it is more efficient to sell the liquidated assets to banks, for this to happen they need to have the liquidity to purchase the assets.

Assumption 2 *Banks can purchase the assets of a liquidated bank only if they are liquid, that is, $b_t < \xi_t l_t$.*

A bank is liquid if it can issue new liabilities at the beginning of the period without renegotiating. Obviously, if the bank starts with $b_t > \xi_t l_t$ —that is, the liabilities are greater than the liquidation value of its assets—the bank will be unable to raise additional funds: potential investors know that the new liabilities (as well as the outstanding liabilities) are not collateralized and the bank will renegotiate immediately after receiving the funds.⁵

To better understand these assumptions, consider the condition for not renegotiating, $b_t \leq \xi_t l_t$, where now $\xi_t \in \{\underline{\xi}, 1\}$ is the liquidation price of bank

⁵Similar assumptions are made in Perri and Quadrini (2011) in a model without banks.

assets at the beginning of the period. If this condition is satisfied, banks have the option to raise additional funds at the beginning of the period to purchase the assets of a defaulting bank. This insures that the market price of the liquidated assets is $\xi_t = 1$. However, if $b_t > \xi_t l_t$ for all banks, there will not be any bank with unused credit. As a result, the liquidated assets can only be sold to non-banks and the price will be $\xi_t = \underline{\xi}$. Therefore, the value of liquidated assets depends on the financial decision of banks, which in turn depends on the expected liquidation value of their assets. This interdependence creates the conditions for multiple self-fulfilling equilibria.

Proposition 2.2 *There exists multiple equilibria if and only if the leverage of the bank is within the two liquidation prices, that is, $\underline{\xi} \leq \omega_t \leq 1$.*

Proof 2.2 *See appendix F.*

Given the multiplicity, I assume that the equilibrium selection takes place stochastically through sunspot shocks. Denote by ε a variable that takes the value of zero with probability λ and 1 with probability $1 - \lambda$. The probability of a low liquidation price, denoted by $\theta(\omega_t)$, is equal to

$$\theta(\omega_t) = \begin{cases} 0, & \text{if } \omega_t < \underline{\xi} \\ \lambda, & \text{if } \underline{\xi} \leq \omega_t \leq 1 \\ 1, & \text{if } \omega_t > 1 \end{cases}$$

If the leverage is sufficiently small ($\omega_t < \underline{\xi}$), banks do not renegotiate even if the liquidation price is low. But then the price cannot be low since banks remain liquid for any expectation of the liquidation price ξ_t and, therefore, for any draw of the sunspot variable ε . Instead, when the leverage is between the two liquidation prices ($\underline{\xi} \leq \omega_t \leq 1$), the liquidity of banks depends on the expectation of this price. Therefore, the equilibrium outcome depends on the realization of the sunspot variable ε . When $\varepsilon = 0$ —which happens with probability λ —the market expects the low liquidation price $\xi_t = \underline{\xi}$, making the banking sector illiquid. On the other hand, when $\varepsilon = 1$ —which happens with probability $1 - \lambda$ —the market expects the high liquidation price $\xi_t = 1$ so that the banking sector remains liquid. The dependence of the probability $\theta(\omega_t)$ on the leverage of the banking sector plays an important role for the results of this paper.

2.6 General equilibrium

To characterize the general equilibrium I first derive the aggregate demand for bank liabilities from the optimal saving of entrepreneurs. I then derive the supply by consolidating the demand of loans from workers with the optimal policy of banks. In this section I assume that the borrowing limit for workers takes the simpler form specified in (2), which allows me to characterize the equilibrium analytically.

Demand for bank liabilities As shown in Lemma 2.1, the optimal saving of entrepreneurs takes the form $b_{t+1}^i/R_t^b = \beta a_t^i$, where a_t^i is the end-of-period wealth $a_t^i = \tilde{b}_t^i + (z_t^i - w_t)h_t^i$. The lemma was derived under the assumption that the bonds purchased by the entrepreneurs were not risky, that is, entrepreneurs receive b_{t+1} units of consumption goods with certainty in the next period $t + 1$. In the extension with financial intermediation, however, bank liabilities are risky since banks may renege on their liabilities. Thanks to the logarithmic utility, however, Lemma 2.1 also holds when the saving instrument is risky.⁶

Since $h_t^i = \phi(w_t)\tilde{b}_t^i$ (see Lemma 2.1), the end-of-period wealth can be rewritten as $a_t^i = [1 + (z_t^i - w_t)\phi(w_t)]\tilde{b}_t^i$. Substituting into the optimal saving and aggregating over all entrepreneurs we obtain

$$B_{t+1} = \beta R_t^b \left[1 + (\bar{z} - w_t)\phi(w_t) \right] \tilde{B}_t. \quad (15)$$

This equation defines the aggregate demand for bank liabilities as a function of the interest rate R_t^b , the wage rate w_t , and the beginning-of-period aggregate wealth of entrepreneurs \tilde{B}_t . Remember that the tilde sign denotes the financial wealth of entrepreneurs after the renegotiation of banks. Also notice that R_t^b is not the expected return from bank liabilities since banks will repay b_{t+1} in full only with some probability.

Using the equilibrium condition in the labor market, we can express the wage rate as a function of \tilde{B}_t . In particular, equalizing the demand for labor, $H_t^D = \phi(w_t)\tilde{B}_t$, to the supply from workers, $H_t^S = (w_t/\alpha)^\nu$, the wage w_t becomes a function of only \tilde{B}_t . We can then use this function to replace w_t in (15) and express the demand for bank liabilities as a function of only \tilde{B}_t and R_t^b . This takes the form

$$B_{t+1} = s(\tilde{B}_t) R_t^b, \quad (16)$$

⁶The proof requires only a trivial extension of the proof of Lemma 2.1 and is omitted.

where $s(\tilde{B}_t)$ is strictly increasing in the wealth of entrepreneurs \tilde{B}_t .

Figure 4 plots this function for a given value of \tilde{B}_t . As we change \tilde{B}_t , the slope of the demand function changes. More specifically, keeping the interest rate constant, higher initial wealth \tilde{B}_t implies higher demand for B_{t+1} .

Supply of bank liabilities The supply of bank liabilities is derived from consolidating the borrowing decisions of workers with the investment and funding decisions of banks.

According to Lemma 2.2, when banks are highly leveraged, that is, $\omega_{t+1} > \underline{\xi}$, the interest rate on loans must be smaller than the intertemporal discount rate ($R_t^l < 1/\beta$). From the workers' first order condition (5) we can see that $\mu_t > 0$ if $R_t^l < 1/\beta$. Therefore, the borrowing constraint for workers is binding, which implies $L_{t+1} = \eta$. Since $B_{t+1} = \omega_{t+1}L_{t+1}$, the supply of bank liabilities is then $B_{t+1} = \eta\omega_{t+1}$.

When the lending rate is equal to the intertemporal discount rate, instead, the demand for loans from workers is undetermined, which in turn implies indeterminacy in the supply of bank liabilities. In this case the liabilities of banks are demand determined. In summary, the supply of bank liabilities is

$$B^s(\omega_{t+1}) = \begin{cases} \text{Undetermined,} & \text{if } \omega_{t+1} < \underline{\xi} \\ \eta\omega_{t+1}, & \text{if } \omega_{t+1} \geq \underline{\xi} \end{cases} \quad (17)$$

So far I have derived the supply of bank liabilities as a function of the bank leverage ω_{t+1} . However, the leverage of banks also depends on the cost of borrowing $\bar{R}_t^b/(1-\tau)$ through condition (13). The average expected return on bank liabilities for investors, \bar{R}_t^b , is in turn related to the interest rate R_t^b by the condition

$$\bar{R}_t^b = \left[1 - \theta(\omega_{t+1}) + \theta(\omega_{t+1}) \left(\frac{\underline{\xi}}{\omega_{t+1}} \right) \right] R_t^b. \quad (18)$$

With probability $1 - \theta(\omega_{t+1})$ banks do not renegotiate and the ex-post return is R_t^b . With probability $\theta(\omega_{t+1})$, however, banks renegotiate and investors recover only a fraction $\underline{\xi}/\omega_{t+1}$ of the initial investment. Therefore, when banks renegotiate, the actual return is $(\underline{\xi}/\omega_{t+1})R_t^b$.

Using (18) to replace \bar{R}_t^b in equation (13) I obtain a function that relates the interest rate R_t^b to the leverage of banks ω_{t+1} . Finally, I combine this

function with $B_{t+1} = \eta\omega_{t+1}$ to obtain the supply of bank liabilities as a function of R_t^b .

Figure 4 plots the supplies of bank liabilities which is undetermined when the interest rate is equal to $(1 - \tau)/\beta$ and strictly decreasing for lower values of the interest rate until it reaches η .

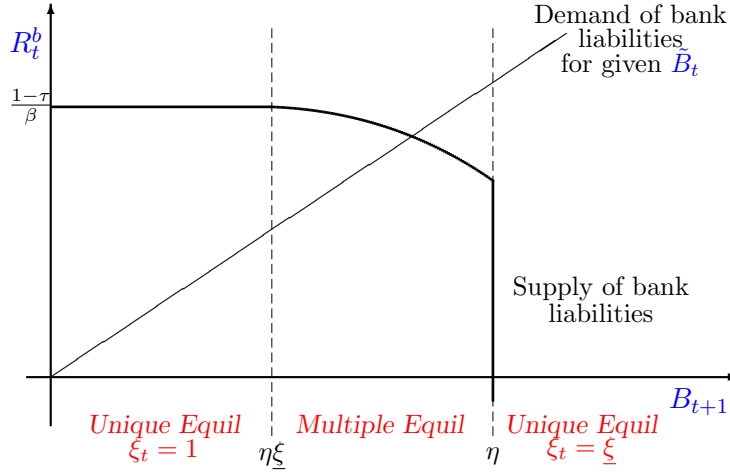


Figure 4: Demand and supply of bank liabilities.

Equilibrium The general equilibrium is characterized by the intersection of the demand and supply of bank liabilities as plotted in Figure 4. The supply (from banks) is decreasing in the funding rate R_t^b while the demand (from entrepreneurs) is increasing in R_t^b . The demand is plotted for a particular value of outstanding post-renegotiation liabilities \tilde{B}_t . By changing the outstanding liabilities, the slope of the demand function changes.

The figure also indicates the regions with unique or multiple equilibria. When the interest rate is $(1 - \tau)/\beta$, banks are indifferent in the choice of leverage $\omega_{t+1} \leq \underline{\xi}$. When the funding rate falls below this value, however, the optimal leverage starts to increase above $\underline{\xi}$ and the economy enters in the region with multiple equilibria. Once the leverage reaches $\omega_{t+1} = 1$, a further decline in the interest rate paid by banks on their liabilities does not lead to higher leverages since the choice of $\omega_{t+1} > 1$ would cause renegotiation with probability 1.⁷

⁷The dependence of the existence of multiple equilibria from the leverage of the economy

Given the initial entrepreneurial wealth \tilde{B}_t , the intersection of demand and supply of bank liabilities determines the interest rate R_t^b , which in turn determines the next period wealth of entrepreneurs \tilde{B}_{t+1} . In absence of renegotiation we have $\tilde{B}_{t+1} = B_{t+1}$, where B_{t+1} is determined by equation (16). In the event of renegotiation (assuming that we are in a region with multiple equilibria) we have $\tilde{B}_{t+1} = (\xi/\omega_{t+1})B_{t+1}$. The new \tilde{B}_{t+1} will determine a new slope for the demand of bank liabilities, and therefore, new equilibrium values of R_t^b and B_{t+1} . Depending on the parameters, the economy may or may not reach a steady state. A key parameter determining the convergence to a steady state is the intermediation cost τ .

Proposition 2.3 *There exists $\hat{\tau} > 0$ such that: If $\tau \geq \hat{\tau}$, the economy converges to a steady state without renegotiation. If $\tau < \hat{\tau}$, the economy never converges to a steady state but switches stochastically between equilibria with and without renegotiation depending to the realization of the sunspot ε .*

Proof 2.3 *See Appendix G*

In order to converge to a steady state, the economy has to reach an equilibrium in which renegotiation never arises. This can happen only if the interest rate paid on bank liabilities is equal to $R_t^b = (1 - \tau)/\beta$. With this interest rate banks do not have incentive to leverage because the funding cost is equal to the return on loans. For this to be an equilibrium, however, the demand for bank liabilities must be sufficiently low which cannot be the case when $\tau = 0$. With $\tau = 0$, in fact, the steady state interest rate must be equal to $1/\beta$. But then entrepreneurs continue to accumulate bank liabilities without bound for precautionary reasons. The demand for bank liabilities will eventually become bigger than the supply (which is bounded by the borrowing constraint of workers), driving the interest rate below $1/\beta$. As the interest rate falls, multiple equilibria become possible.

Bank leverage and crises Figure 4 illustrates how the type of equilibria depends on the bank leverage. When banks increase their leverage, the economy switches from a state in which the equilibrium is unique (no crises) to a state with multiple equilibria (and the possibility of financial crises). But even if the economy was already in a state with multiple equilibria, the increase in leverage implies that the consequences of a crisis are bigger. In

is also a feature of the sovereign default model of Cole and Kehoe (2000).

fact, when the economy switches from a good equilibria to a bad equilibria, the bank liabilities are renegotiated to $\eta\xi$. Therefore, bigger are the liabilities issued by banks and larger are the losses incurred by entrepreneurs holding these liabilities. Larger financial losses incurred by entrepreneurs then imply larger declines in the demand for labor, which in turn cause larger macroeconomic contractions. In the next section I will examine two recent trends that may have increased the incentives of banks to take more leverage.

3 The growth of emerging countries

As shown in the introduction, emerging countries have experienced an unprecedented economic growth together with a sizable increase in the foreign holdings of safer financial assets issued by industrialized countries. The goal of this section is to study how the increased demand for financial assets by emerging countries has affected the financial and macroeconomic stability of industrialized countries.

To investigate this issue, I interpret the model as representative of industrialized countries. The model is extended by assuming that there is an *exogenous* foreign demand for the bank liabilities. Therefore, the total demand for liabilities issued by banks of industrialized countries is the sum of the demand coming from domestic entrepreneurs (which is endogenous) and from foreign countries (which is exogenous). The exogeneity of the foreign demand means that this demand is insensitive to changes in the equilibrium interest rate.

Denoting by B_t^D the domestic demand and by B_t^F the foreign demand, the total demand for bank liabilities is equal to $B_t = B_t^D + B_t^F$. The renegotiation condition for banks remains $B_t > \xi_t L_t$. Besides this, the structure of the economy and the equilibrium conditions are the same as in the closed-economy model studied earlier. For the analysis of this section, which is based on numerical simulations, I use the borrowing limit specified in 3. This specification of the borrowing constraint allows for the price of the fixed asset to fluctuate over time so that I can also study how the inflow of foreign capital affects the dynamics of asset prices.

Parametrization. The period in the model is a quarter and the discount factor is set to $\beta = 0.9825$, implying an annual intertemporal discount rate of about 7%. The parameter ν in the utility function of workers is the

elasticity of the labor supply. I set this elasticity to the high value of 50. The reason to use this high value is to capture, in a simple way, possible wage rigidities. In fact, with a very high elasticity of the labor supply, wages are almost constant. The alternative would be to model explicitly downward wage rigidities but this requires an additional state variable and would make the computation of the model more demanding. The utility parameter α is chosen to have an average working time of 0.3.

The average productivity of entrepreneurs is normalized to $\bar{z} = 1$. Since the average input of labor is 0.3, the average production is also 0.3. The supply of the fixed asset is normalized to $\bar{k} = 1$ and its production flow is set to $\chi = 0.05$. Total production is the sum of entrepreneurial production (0.3) plus the production from the fixed asset (0.05). Therefore, total production is 0.35 per quarter (about 1.4 per year).

The parameter η determines the fraction of the fixed asset that can be used as a collateral. This is set to 0.6. The productivity shock follows a truncated normal distribution with standard deviation of 0.3. Given the baseline parametrization, this implies that the standard deviation of entrepreneurial wealth is about 7%.

The parameters that pertain to the banking sector are chosen as follows. The low value of ξ is set to $\underline{\xi} = 0.75$. The probability that the sunspot variable ε takes the value of zero (which could lead to a bank crisis) is set to 2 percent ($\lambda = 0.02$). Therefore, provided that the economy is in a region that admits multiple equilibria, a crisis arises on average every fifty quarters. The renegotiation cost is assumed to be quadratic, that is, $\varphi(.) = (.)^2$. Finally, the operation cost for banks is set to $\tau = 0.0045$.

At this point we are left with the parametrization of the foreign demand for bank liabilities. This is chosen to replicate the net foreign asset position of industrialized countries in debt and international reserves as shown in Figure 1 for the period 1990-2011. Before 1990, I assume that the net position is constant at the 1990 level, that is, -3.2% of output. Then during the subsequent period 1991-2011 it follows the exact pattern shown in the data. Since the period in the model is a quarter while the data on net foreign asset positions is available annually, the inter-quarter values are assumed to be equal to the annual levels. Starting in 2012, I assume that the net position remains at the 2011 level, that is, -20% of GDP. Of course, it is unknown what the future pattern will be and I could make alternative assumptions. But this will not change in important ways the dynamics during the period of interest, that is, 1991-2011. I assume further that until 1990, the growth

in the external demand for bank liabilities is not anticipated. Starting in 1991, however, the future pattern of the foreign demand for bank liabilities is perfectly predicted.

Numerical exercise and results. Given the parameter values described above, I simulate the model for 2,000 quarters (500 years) using a random sequence of draws of the sunspot shock. In the first 1,000 quarters the foreign demand for bank liabilities is fixed at the 1990 level and agents do not anticipate the future growth in demand. Starting at quarter 1,001 (which corresponds to the first quarter of 1991), agents learn that the foreign demand has changed and will continue to change during the next 80 quarters (from 1991 to 2011) after which it stabilizes at the level observed in 2011. Therefore, the break period is the first quarter of 1991.

Since there are sunspot shocks that could shift the economy from one type of equilibrium to the other, the dynamics of the economy depend on the actual realizations of the shock. To better illustrate the stochastic nature of the model, I repeat the simulation of the model 1,000 times (with each simulation performed over 2,000 periods as described above). Figure 5 plots the average of the 1,000 repeated simulations as well as the 5th and 95th percentiles in each quarter over the period 1981-2020. This corresponds to periods 960 to 1,120 in each simulation. The range of variation between the 5th and 95th percentiles provides information about the volatility of the economy at any point in time.

The first panel plots the foreign demand for bank liabilities. The foreign demand is exogenous in the model and the 1991 change determines a structural break. The next five panels plot five endogenous variables: the total liabilities of banks (domestically and foreign held), their leverage, the lending rate, the price of the fixed asset and the input of labor.

The first point to notice is that, following the increase in foreign demand, the interval delimited by the 5th and 95th percentiles for the repeated simulations widens dramatically. Therefore, financial and macroeconomic volatility increases substantially as we move to the 2000s. In this particular simulation, the probability of a bank crisis is always positive, even before the structural break induced by the change in foreign demand for bank liabilities in the early 1990s. However, after the structural change, the consequence of a bank crisis could be much bigger since the distance between the 5th and 95th percentiles is significantly wider.

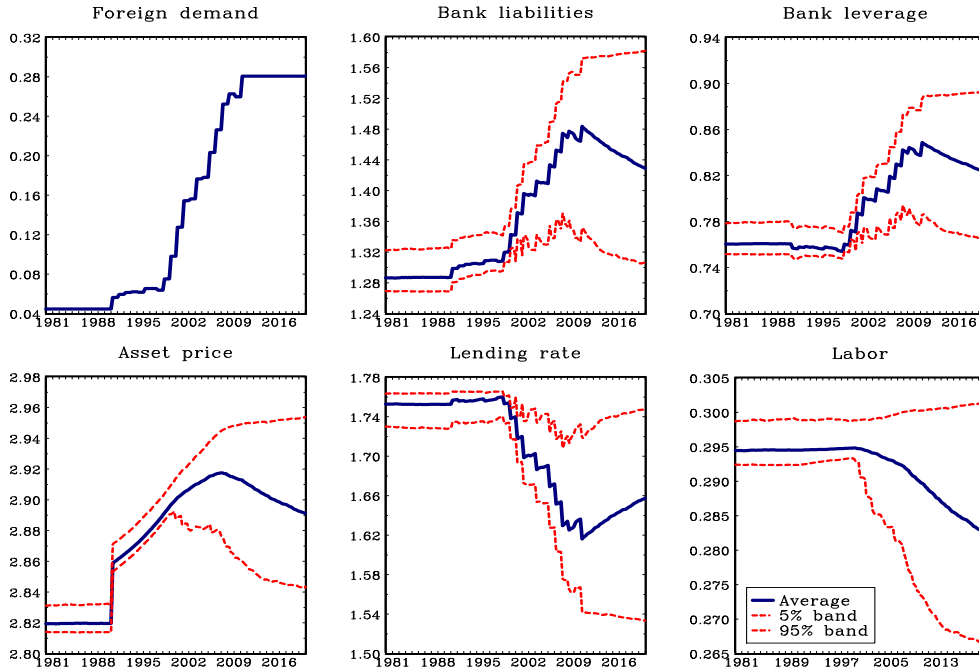


Figure 5: Change in foreign demand for bank liabilities. Responses of 1,000 simulations.

Besides the increase in financial and macroeconomic volatility, the figure reveals other interesting patterns. First, as the foreign demand increases, banks raise their leverage while the interest rate on loans decreases. The economy also experiences an increase in asset prices (the price of the fixed asset) but labor declines on average. This is a consequence of the decline in labor demand. As the foreign demand for bank liabilities increases, part of the increase is filled with lower holdings of bank liabilities by domestic entrepreneurs (in addition to higher bank leverage). But as domestic entrepreneurs hold less financial wealth, they become more averse to take the risk associated with hiring.

It is important to point out that, although labor falls in the average of all repeated simulations, the actual dynamics of labor during the 20 years that followed the 1991 break could be increasing or decreasing depending on the actual realizations of the sunspot shocks. To show this point, I repeat the experiment shown in Figure 5 but for a particular sequence of sunspot shocks. In particular, I simulate the model under the assumption that, starting in the first quarter of 1991, the economy experiences a sequence of draws of the

sunspot variable $\varepsilon = 1$ until the second quarter of 2008. Then in the third quarter of 2008 the draw of the sunspot shock becomes $\varepsilon = 0$ but returns to $\varepsilon = 1$ from the fourth quarter of 2008 and in all subsequent quarters.

This particular sequence of draws captures the idea that expectations may have turned pessimistic in the fourth quarter of 2008 leading to a sudden financial and macroeconomic crisis. The statistics for the resulting simulation is reported in Figure 6. The continuous line is still the average at time t of the 1,000 simulations. However, differently from the previous graph, starting from the first quarter of 1991 the sequences of draws for the sunspot variable is always the same for all 1,000 repeated simulations.

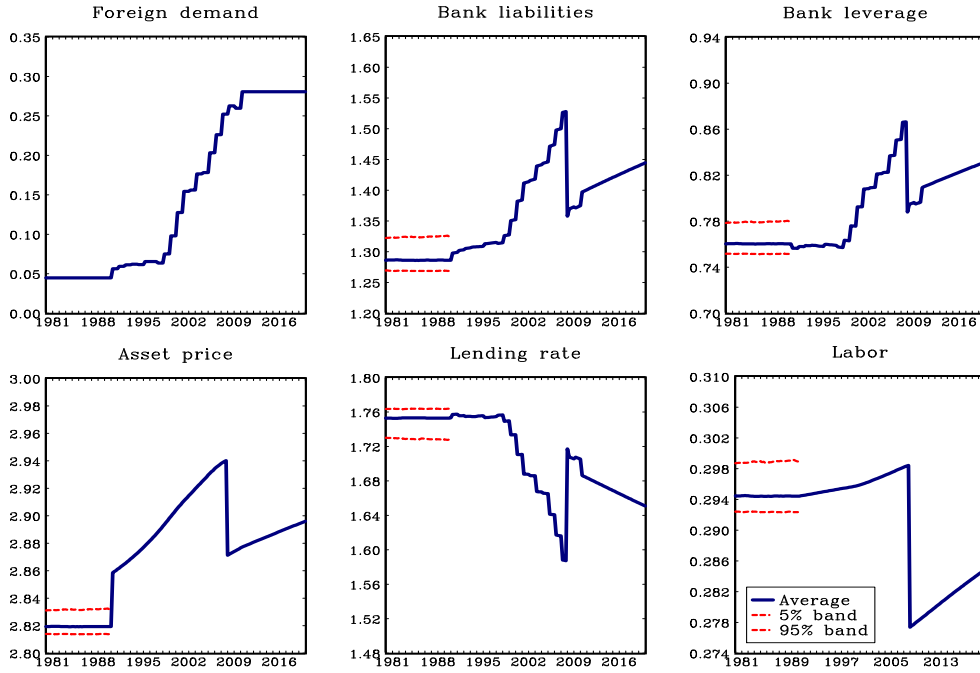


Figure 6: Change in foreign demand for bank liabilities. Responses of 1,000 simulations with same draws of the sunspot variable starting in 1991.

As we can see from Figure 6, even if the demand for bank liabilities from the foreign sector increases, as long as the draws of the sunspot variable is $\varepsilon = 1$, asset prices continue to increase and the input of labor does not drop. However, a single realization $\varepsilon = 1$ of the sunspot shock can trigger a large decline in labor. Furthermore, even if the negative shock is only for one period and there are no crises afterwards, the recovery in the labor market

is extremely slow. This is because the crisis generates a large decline in the financial wealth of employers and it will take a long time for them to rebuild the lost wealth through savings.

Another way of showing the importance of the growth of emerging countries for macroeconomic stability in industrialized countries, is by conducting the following counterfactual exercise. I repeat the simulation shown in Figure 6 but under the assumption that the foreign demand for bank liabilities remains at the pre-1991 level for the whole simulation period. This counterfactual exercise tells us how the financial and macroeconomic dynamics in response to the same shocks would have changed in absence of the observed increase in foreign demand for bank liabilities. The resulting simulation is shown in Figure 7.

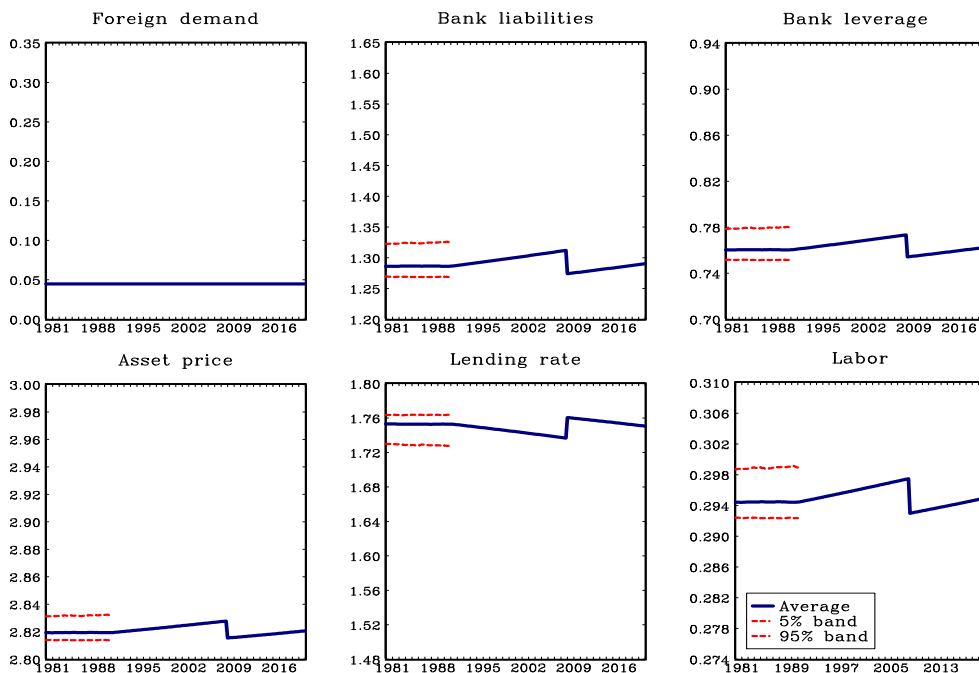


Figure 7: Counterfactual exercise with constant foreign demand for bank liabilities. Responses of 1,000 simulations with same draws of the sunspot variable starting in 1991.

As shown in the figure, without the increase in foreign demand for bank liabilities, the same sequence of sunspot shocks would have generated a much smaller financial and macroeconomic expansion before 2008 as well as a much smaller contraction in the third quarter of 2008. Therefore, the increase in

foreign demand for financial assets issued by industrialized countries could have contributed to the observed expansion of the financial sector in industrialized countries but it also created the conditions for greater financial and macroeconomic fragility that became evident once the crisis materialized.

4 Discussion and conclusion

The sustained high growth experienced by emerging economies has increased their share of the world economy. An implication of this is that the economic performance of these countries is becoming more and more important for the performance of industrialized countries. The view that emerging countries are a collection of small open economies that are highly dependent on industrialized countries but they are of negligible importance for industrialized economies is no longer valid. The recent growth of emerging countries has made this view obsolete.

There are many channels through which emerging economies could affect industrialized countries and in this paper I emphasized one of these channels: the increased external demand for financial assets issued by industrialized countries. In particular, I have shown that the increased demand for financial assets raises the incentives of financial intermediaries in industrialized countries to leverage. On the one hand, this allows for the expansion of the financial sector with positive effects on real macroeconomic variables. On the other, it increases the fragility of the financial system, raising the probability and/or the consequences of a crisis.

These results are illustrated with a model in which the banking sector plays a central role in the intermediation of funds and, therefore, in the creation of financial assets. The paper emphasizes a special channel through which banks can affect the real sector of the economy: the issuance of liabilities held by the nonfinancial sector for insurance purposes. When the supply of bank liabilities or their value are low, agents are less willing to engage in risky activities and this causes a macroeconomic contraction.

The analysis of the paper also shows that booms and busts in financial intermediation can be driven by self-fulfilling expectations about the liquidity of the banking sector. When the economy expects the banking sector to be liquid, banks have an incentive to leverage and this allows for an economic boom. But as the leverage increases, the banking sector becomes vulnerable to pessimistic expectations about its liquidity, creating the conditions for a financial crisis. The increase in external demand for financial assets

from emerging economies amplifies this mechanism because, by reducing the funding cost, it increases the incentive of banks to leverage.

In reality, financial assets that can be held for precautionary reasons are also created directly in nonfinancial sectors. For example, firms and governments issue liabilities that are directly held by nonfinancial sectors. Still, financial intermediaries play an important role in the direct issuance of these instruments such as corporate and government bonds. Financial intermediaries also play an important role in the secondary market for these instruments. Therefore, difficulties in financial intermediation is likely to affect the functioning and valuation of all financial markets. It is for this reason that in this paper I focused on the operation of financial intermediaries.

An important feature of the model economy studied here is that the expansion of the financial sector improves the allocation efficiency. This is because the issuance of bank liabilities provides insurance instruments for entrepreneurs, encouraging them to hire more labor. However, the expansion of the financial sector is associated with higher leverage, making the financial system more vulnerable to crises. Therefore, from a policy perspective, there is a trade-off: allowing for the expansion of the macro-economy at the cost of deeper crises. The study of optimal policies will be a subject a future research.

Appendix

A Proof of Lemma 2.1

The optimization problem of an entrepreneur can be written recursively as

$$\begin{aligned} V_t(b_t) &= \max_{h_t} \mathbb{E}_t \tilde{V}_t(a_t) & (19) \\ &\text{subject to} \\ &a_t = b_t + (z_t - w_t)h_t \end{aligned}$$

$$\begin{aligned} \tilde{V}_t(a_t) &= \max_{b_{t+1}} \left\{ \ln(c_t) + \beta \mathbb{E}_t V_{t+1}(b_{t+1}) \right\} & (20) \\ &\text{subject to} \\ &c_t = a_t - \frac{b_{t+1}}{R_t} \end{aligned}$$

Since the information set changes from the beginning of the period to the end of the period, the optimization problem has been separated according to the available information. In sub-problem (19) the entrepreneur chooses the input of labor without knowing the productivity z_t . In sub-problem (20) the entrepreneur allocates the end of period wealth in consumption and savings after observing z_t .

The first order condition for sub-problem (19) is

$$\mathbb{E}_t \frac{\partial \tilde{V}_t}{\partial a_t} (z_t - w_t) = 0.$$

The envelope condition from sub-problem (20) gives

$$\frac{\partial \tilde{V}_t}{\partial a_t} = \frac{1}{c_t}.$$

Substituting in the first order condition we obtain

$$\mathbb{E}_t \left(\frac{z_t - w_t}{c_t} \right) = 0. \quad (21)$$

At this point we proceed by guessing and verifying the optimal policies for employment and savings. The guessed policies take the form:

$$h_t = \phi_t b_t \quad (22)$$

$$c_t = (1 - \beta) a_t \quad (23)$$

Since $a_t = b_t + (z_t - w_t)h_t$ and the employment policy is $h_t = \phi_t b_t$, the end of period wealth can be written as $a_t = [1 + (z_t - w_t)\phi_t]b_t$. Substituting in the guessed consumption policy we obtain

$$c_t = (1 - \beta) \left[1 + (z_t - w_t)\phi_t \right] b_t. \quad (24)$$

This expression is used to replace c_t in the first order condition (21) to obtain

$$\mathbb{E}_t \left[\frac{z_t - w_t}{1 + (z_t - w_t)\phi_t} \right] = 0, \quad (25)$$

which is the condition stated in Lemma 2.1.

To complete the proof, we need to show that the guessed policies (22) and (23) satisfy the optimality condition for the choice of consumption and saving. This is characterized by the first order condition of sub-problem (20), which is equal to

$$-\frac{1}{c_t R_t} + \beta \mathbb{E}_t \frac{\partial V_{t+1}}{\partial b_{t+1}} = 0.$$

From sub-problem (19) we derive the envelope condition $\partial V_t / \partial b_t = 1/c_t$ which can be used in the first order condition to obtain

$$\frac{1}{c_t} = \beta R_t \mathbb{E}_t \frac{1}{c_{t+1}}.$$

We have to verify that the guessed policies satisfy this condition. Using the guessed policy (23) and equation (24) updated one period, the first order condition can be rewritten as

$$\frac{1}{a_t} = \beta R_t \mathbb{E}_t \frac{1}{[1 + (z_{t+1} - w_{t+1})\phi_{t+1}]b_{t+1}}.$$

Using the guessed policy (23) we have that $b_{t+1} = \beta R_t a_t$. Substituting and rearranging we obtain

$$1 = \mathbb{E}_t \left[\frac{1}{1 + (z_{t+1} - w_{t+1})\phi_{t+1}} \right]. \quad (26)$$

The final step is to show that, if condition (25) is satisfied, then condition (26) is also satisfied. Let's start with condition (25), updated by one period. Multiplying both sides by ϕ_{t+1} and then subtracting 1 in both sides we obtain

$$\mathbb{E}_{t+1} \left[\frac{(z_{t+1} - w_{t+1})\phi_{t+1}}{1 + (z_{t+1} - w_{t+1})\phi_{t+1}} - 1 \right] = -1.$$

Multiplying both sides by -1 and taking expectations at time t we obtain (26).

B Proof of Proposition 2.1

As shown in Lemma 2.1, the optimal saving of entrepreneurs takes the form $b_{t+1}^i/R_t^b = \beta a_t^i$, where a_t^i is the end-of-period wealth $a_t^i = b_t^i + (z_t^i - w_t)h_t^i$. Since $h_t^i = \phi(w_t)b_t^i$ (see Lemma 2.1), the end-of-period wealth can be rewritten as $a_t^i = [1 + (z_t^i - w_t)\phi(w_t)]b_t^i$. Substituting into the optimal saving and aggregating over all entrepreneurs we obtain

$$B_{t+1} = \beta R_t^b \left[1 + (\bar{z} - w_t)\phi(w_t) \right] B_t. \quad (27)$$

This equation defines the aggregate demand for bonds as a function of the interest rate R_t^b , the wage rate w_t , and the beginning-of-period aggregate wealth of entrepreneurs B_t . Notice that the term in square brackets is bigger than 1. Therefore, in a steady state equilibrium where $B_{t+1} = B_t$, the condition $\beta R < 1$ must be satisfied.

Using the equilibrium condition in the labor market, I can express the wage rate as a function of B_t . In particular, equalizing the demand for labor, $H_t^D = \phi(w_t)\tilde{B}_t$, to the supply from workers, $H_t^S = (w_t/\alpha)^\nu$, the wage w_t can be expressed as a function of only \tilde{B}_t . We can then use this function to replace w_t in (27) and express the demand for bank liabilities as a function of only B_t and R_t^b as follows

$$B_{t+1} = s(B_t) R_t^b. \quad (28)$$

The function $s(B_t)$ is strictly increasing in the wealth of entrepreneurs, B_t .

Consider now the supply of bonds from workers. For simplicity I assume that the borrowing constraint takes the form specified in equation (2), that is, $l_{t+1} \leq \eta$. Using this limit together with the first order condition (5), we have that, either the interest rate satisfies $1 = \beta R_t^b$ or workers are financially constrained, that is, $B_{t+1} = \eta$. When the interest rate is equal to the inter-temporal discount rate (first case), we can see from (27) that $B_{t+1} > B_t$. So eventually, the borrowing constraint of workers becomes binding, that is, $B_{t+1} = \eta$ (second case). When the borrowing constraint is binding, the multiplier μ_t is positive and condition (5) implies that the interest rate is smaller than the inter-temporal discount rate. So the economy has reached a steady state. The steady state interest rate is determined by condition (28) after setting $B_t = B_{t+1} = \eta$. This is the only steady state equilibrium.

When the borrowing constraint takes the form (3), the proof is more involved but the economy also reaches a steady state with $\beta R < 1$.

C First order conditions for workers

The optimization problem of a worker can be written recursively as

$$\begin{aligned}
 V_t(l_t, k_t) &= \max_{h_t, l_{t+1}, k_{t+1}} \left\{ c_t - \alpha \frac{h_t^{1+\frac{1}{\nu}}}{1 + \frac{1}{\nu}} + \beta V_{t+1}(l_{t+1}, k_{t+1}) \right\} \\
 &\text{subject to} \\
 c_t &= w_t h_t + \chi k_t + \frac{l_{t+1}}{R_t^l} - l_t - (k_{t+1} - k_t) p_t \\
 \eta &\geq l_{t+1}.
 \end{aligned}$$

Given $\beta\mu_t$ the lagrange multiplier associated with the borrowing constraint, the first order conditions with respect to h_t , l_{t+1} , k_{t+1} are, respectively,

$$\begin{aligned}
 -\alpha h_t^{\frac{1}{\nu}} + w_t &= 0, \\
 \frac{1}{R_t^l} + \beta \frac{\partial V_{t+1}(l_{t+1}, k_{t+1})}{\partial l_{t+1}} - \beta\mu_t &= 0, \\
 -p_t + \beta \frac{\partial V_{t+1}(l_{t+1}, k_{t+1})}{\partial k_{t+1}} &= 0.
 \end{aligned}$$

The envelope conditions are

$$\begin{aligned}
 \frac{\partial V_t(l_{t+1}, k_{t+1})}{\partial l_{t+1}} &= -1, \\
 \frac{\partial V_t(l_{t+1}, k_{t+1})}{\partial k_{t+1}} &= \chi + p_t.
 \end{aligned}$$

Updating by one period and substituting in the first order conditions we obtain (4), (5), (6).

When the borrowing constraint takes the form $\eta \mathbb{E}_t p_{t+1} k_{t+1} \geq l_{t+1}$, the first order condition with respect to k_{t+1} becomes

$$-p_t + \beta \frac{\partial V_{t+1}(l_{t+1}, k_{t+1})}{\partial k_{t+1}} + \eta \beta \mu_t \mathbb{E}_t p_{t+1} = 0,$$

Substituting the envelope condition we obtain (7).

D First order conditions for problem (12)

The first order conditions for problem (12) with respect to b_{t+1} and l_{t+1} are

$$\frac{1-\tau}{\bar{R}_t^b} \mathbb{E}_t \frac{\partial \tilde{b}_{t+1}}{\partial b_{t+1}} = \beta \mathbb{E}_t \left[\frac{\partial \tilde{b}_{t+1}}{\partial b_{t+1}} + \frac{\partial \tilde{\varphi}_{t+1}}{\partial b_{t+1}} + \gamma_t \right] \quad (29)$$

$$\frac{1}{R_t^l} = \frac{1-\tau}{\bar{R}_t^b} \mathbb{E}_t \frac{\partial \tilde{b}_{t+1}}{\partial l_{t+1}} + \beta \mathbb{E}_t \left[1 - \frac{\partial \tilde{b}_{t+1}}{\partial l_{t+1}} - \frac{\partial \tilde{\varphi}_{t+1}}{\partial l_{t+1}} + \gamma_t \right], \quad (30)$$

where γ_t is the Lagrange multiplier associated with constraint $b_{t+1} \leq l_{t+1}$.

I now use the definition of \tilde{b}_{t+1} and $\tilde{\varphi}_{t+1}$ provided in equations (8) and (9) to derive the following terms

$$\begin{aligned} \mathbb{E}_t \frac{\partial \tilde{b}_{t+1}}{\partial b_{t+1}} &= 1 - \theta(\omega_{t+1}), \\ \mathbb{E}_t \frac{\partial \tilde{b}_{t+1}}{\partial l_{t+1}} &= \theta(\omega_{t+1}) \underline{\xi}, \\ \mathbb{E}_t \frac{\partial \tilde{\varphi}_{t+1}}{\partial b_{t+1}} &= \theta(\omega_{t+1}) \left[\varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1} + \varphi(\omega_{t+1} - \underline{\xi}) \right], \\ \mathbb{E}_t \frac{\partial \tilde{\varphi}_{t+1}}{\partial l_{t+1}} &= -\theta(\omega_{t+1}) \varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1}^2, \end{aligned}$$

where $\theta(\omega_{t+1})$ is the probability of renegotiation defined as

$$\theta(\omega_{t+1}) = \begin{cases} 0, & \text{if } \omega_{t+1} < \underline{\xi} \\ \lambda, & \text{if } \underline{\xi} \leq \omega_{t+1} \leq 1 \\ 1, & \text{if } \omega_{t+1} > 1 \end{cases}$$

Substituting in (29) and (30) and re-arranging we obtain

$$\frac{1-\tau}{\bar{R}_t^b} = \beta \left[1 + \frac{\theta(\omega_{t+1}) \left(\varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1} + \varphi(\omega_{t+1} - \underline{\xi}) \right) + \gamma_t}{1 - \theta(\omega_{t+1})} \right], \quad (31)$$

$$\frac{1}{R_t^l} = \beta \left[1 + \theta(\omega_{t+1}) \varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1}^2 + \left(\frac{1-\tau}{\beta \bar{R}_t^b} - 1 \right) \theta(\omega_{t+1}) \underline{\xi} + \gamma_t \right] \quad (32)$$

where the multiplier γ_t is zero if $\omega_{t+1} < 1$ and positive if $\omega_{t+1} = 1$. Eliminating γ_t we obtain (13) and (14) which can be satisfied with the inequality sign if $\gamma_t > 0$.

E Proof of Lemma 2.2

Let's consider the first order conditions (31) and (32). When $\omega_{t+1} < \underline{\xi}$, the default probability is $\theta(\omega_{t+1}) = 0$ and the first order conditions are satisfied with equality. Therefore, they simplify to

$$\begin{aligned}\frac{1-\tau}{\bar{R}_t^b} &= \beta, \\ \frac{1}{R_t^l} &= \beta,\end{aligned}$$

which proves the first part of the lemma.

Now suppose that $\omega_{t+1} > \underline{\xi}$. In this case the probability of default is $\theta(\omega_{t+1}) = \lambda$ and the first order conditions can be written as

$$\frac{1-\tau}{\bar{R}_t^b} = \beta \left[1 + \frac{\lambda\varphi'(\omega_{t+1} - \underline{\xi})\omega_{t+1} + \lambda\varphi(\omega_{t+1} - \underline{\xi}) + \gamma_t}{1-\lambda} \right], \quad (33)$$

$$\frac{1}{R_t^l} = \beta \left[1 + \lambda\varphi'(\omega_{t+1} - \underline{\xi})\omega_{t+1}^2 + \lambda\underline{\xi} \left(\frac{1-\tau}{\beta\bar{R}_t^b} - 1 \right) + \gamma_t \right], \quad (34)$$

where the multiplier γ_t is bigger than zero if $\omega_{t+1} = 1$.

That $\bar{R}_t^b/(1-\tau)$ and R_t^l are both smaller than $1/\beta$ is obvious from the above two conditions. What is not immediate to see is that $\bar{R}_t^b/(1-\tau) < R_t^l$. To show this, let's first use equation (33) to eliminate \bar{R}_t^b in equation (34). After some re-arrangement I can rewrite equation (34) as

$$\frac{1}{R_t^l} = \beta \left[1 + \frac{\lambda\varphi'(\omega_{t+1} - \underline{\xi})\omega_{t+1}\mathbf{K}_1 + \lambda\varphi(\omega_{t+1} - \underline{\xi})\mathbf{K}_2 + \gamma_t\mathbf{K}_3}{1-\lambda} \right], \quad (35)$$

where

$$\begin{aligned}\mathbf{K}_1 &= (1-\lambda)\omega_{t+1} + \lambda\underline{\xi}, \\ \mathbf{K}_2 &= \lambda\underline{\xi}, \\ \mathbf{K}_3 &= 1-\lambda + \lambda\underline{\xi}.\end{aligned}$$

Because ω_{t+1} , $\underline{\xi}$ and λ are all smaller than 1, the terms \mathbf{K}_1 , \mathbf{K}_2 and \mathbf{K}_3 are also smaller than 1.

To prove that $\bar{R}_t^b/(1-\tau) < R_t^l$ I need to show that the right-hand-side of (33) is bigger than the right-hand-side of (35). This requires to show that

$$\begin{aligned}\lambda\varphi'(\omega_{t+1} - \underline{\xi})\omega_{t+1} + \lambda\varphi(\omega_{t+1} - \underline{\xi}) + \gamma_t &> \\ \lambda\varphi'(\omega_{t+1} - \underline{\xi})\omega_{t+1}\mathbf{K}_1 + \lambda\varphi(\omega_{t+1} - \underline{\xi})\mathbf{K}_2 + \gamma_t\mathbf{K}_3.\end{aligned}$$

This follows directly from \mathbf{K}_1 , \mathbf{K}_2 and \mathbf{K}_3 being smaller than 1.

F Proof of Proposition 2.2

Banks make decisions at two different stages. At the beginning of the period they choose whether to renegotiate the debt and at the end of the period they choose the funding and lending policies. Given the initial states, b_t and l_t , the renegotiation decision boils down to a take-it or leave-it offer made by each bank to its creditors for the repayment of the debt. Denote by $\tilde{b}_t = f(b_t, l_t, \xi_t^e)$ the offered repayment. This depends on the individual liabilities b_t , individual assets l_t , and the expected liquidation price of assets ξ_t^e . The superscript e is to make clear that the bank decision depends on the expected price in the eventuality of liquidation. Obviously, the best repayment offer made by the bank is

$$f(b_t, l_t, \xi_t^e) = \begin{cases} b_t, & \text{if } b_t \leq \xi_t^e l_t \\ \xi_t^e l_t, & \text{if } b_t > \xi_t^e l_t \end{cases}, \quad (36)$$

which is accepted by creditors whenever the actual liquidation price is bigger than the expected price ξ_t^e .

After the renegotiation stage, banks choose the funding and lending policies, b_{t+1} and l_{t+1} . These policies depend on the two interest rates, \bar{R}_t^b and R_t^l , and on the probability distribution of the next period liquidation price ξ_{t+1} . Since we could have multiple equilibria, the next period price could be stochastic. Suppose that the price could take two values, $\underline{\xi}$ and 1, with the probability of the low value defined as

$$\theta(\omega_{t+1}) = \begin{cases} 0, & \text{if } \omega_{t+1} < \underline{\xi} \\ \lambda, & \text{if } \underline{\xi} \leq \omega_{t+1} \leq 1 \\ 1, & \text{if } \omega_{t+1} > 1. \end{cases}$$

The variable $\omega_{t+1} = b_{t+1}/l_{t+1}$ represents the leverage of all banks in a symmetric equilibrium, that is, they all choose the same leverage. For the moment the symmetry of the equilibrium is an assumption. I will then show below that in fact banks do not have incentives to deviate from the leverage chosen by other banks.

Given the above assumption about the probability distribution of the liquidation price, the funding and lending policies of the bank are characterized in Lemma 2.2 and depend on \bar{R}_t^b and R_t^l . In short, if $\bar{R}_t^b/(1-\tau) = R_t^l$, then the optimal policy of the bank is to choose a leverage $\omega_{t+1} \leq \underline{\xi}$. If $\bar{R}_t^b/(1-\tau) < R_t^l$, the optimal leverage is $\omega_{t+1} > \underline{\xi}$.

Given the assumption that the equilibrium is symmetric (all banks choose the same leverage ω_{t+1}), multiple equilibria arise if the chosen leverage is $\omega_{t+1} \in \{\underline{\xi}, 1\}$.

In fact, once we move to the next period, if the market expects $\xi_{t+1}^e = \underline{\xi}$, all banks are illiquid and they choose to renege on their liabilities (given the renegotiation policy (36)). As a result, there will not be any bank that can buy the liquidated assets of other banks. Then the only possible price that is consistent with the expected price is $\xi_{t+1} = \underline{\xi}$. On the other hand, if the market expects $\xi_{t+1}^e = 1$, banks are liquid and, if one bank reneges, creditors can sell the liquidated assets to other banks at the price $\xi_{t+1} = 1$. Therefore, it is optimal for banks not to renegotiate consistently with the renegotiation policy (36).

The above proof, however, assumes that the equilibrium is symmetric, that is, all banks choose the same leverage. To complete the proof, we have to show that there is no incentive for an individual bank to deviate from the leverage chosen by other banks. In particular, I need to show that, in the anticipation that the next period liquidation price could be $\xi_{t+1} = \underline{\xi}$, a bank do not find convenient to chose a lower leverage so that, in the eventuality that the next period price is $\xi_{t+1} = \underline{\xi}$, the bank could purchase the liquidated asset at a price lower than 1 and make a profit (since the unit value for the bank of the liquidated assets is 1).

If the price at $t + 1$ is $\xi_{t+1} = \underline{\xi}$, a liquid bank could offer a price $\underline{\xi} + \epsilon$, where ϵ is a small but positive number. Since the repayment offered by a defaulting bank is $\underline{\xi}_{t+1}$, creditors prefer to sell the assets rather than accepting the repayment offered by the defaulting bank. However, if this happens, the expectation of the liquidation price $\xi^e = \underline{\xi}$ turns out to be incorrect ex-post. Therefore, the presence of a single bank with liquidity will raise the expected liquidation price to $\underline{\xi} + \epsilon$. But even with this new expectation, a bank with liquidity can make a profit by offering $\underline{\xi} + 2\epsilon$. Again, this implies that the expectation turns out to be incorrect ex-post. This mechanism will continue to raise the expected price to $\xi_{t+1}^e = 1$. At this point the liquid bank will not offer a price bigger than 1 and the ex-post liquidation price is correctly predicted to be 1. Therefore, as long as there is a single bank with liquidity, the expected liquidation price must be 1. But then a bank cannot make a profit in period $t + 1$ by choosing a lower leverage in period t with the goal of remaining liquid in the next period. This proves that there is no incentive to deviate from the policy chosen by other banks.

Finally, the fact that multiple equilibria cannot arise when $\omega_t < \underline{\xi}$ is obvious. Even if the price is $\underline{\xi}$, banks remain liquid.

G Proof of Proposition 2.3

Given a fixed interest rate R^b , the aggregate demand for bank liabilities, equation (16), has a converging fix point $B^*(R^b)$. The fixed point is increasing in R^b and converges to infinity as R^b converges to $1/\beta$. This implies that, if $\tau = 0$, then the leverage of banks is always bigger than $\underline{\xi}$. To show this, suppose that banks

choose a leverage of $\omega < \underline{\xi}$. According to conditions (13) and (14), we have that $R^b = R^l = 1/\beta$. But when $R^b = 1/\beta$ the demand of bank liabilities is unbounded in the limit. This implies that to reach a stable equilibrium without renegotiation (that is, $\omega < \underline{\xi}$), R^b must be smaller than $1/\beta$. This requires τ to be sufficiently big. In fact, when $\tau > 0$ and $\omega < \underline{\xi}$, we have $R^b/(1 - \tau) = R^l = 1/\beta$. Since the demand for bank liabilities is increasing in R^b , there must be some $\hat{\tau} > 0$ such that, for $\tau > \hat{\tau}$, the equilibrium is characterized by $\omega < \underline{\xi}$. This implies that the economy is not subject to crises and converges to a steady state. For $\tau < \hat{\tau}$, instead, the equilibrium is characterized by $\omega > \underline{\xi}$. In this case the economy is subject to self-fulfilling crises and, therefore, it does not converge to a steady state.

H Numerical solution

I describe the numerical procedure to solve the model with the endogenous borrowing constraint specified in (3). I first describe the numerical procedure when the external demand for bank liabilities is fixed (without loss of generality set to zero). In this case I can solve for the stochastic stationary equilibrium. I will then describe the numerical procedure when the external demand for bank liabilities changes over time, inducing a transition dynamics.

H.1 Stationary equilibrium without structural break

The states of the economy are given by the bank liabilities B_t , the bank loans L_t and the realization of the sunspot shock ε_t . These three variables are important in determining the renegotiation liabilities \tilde{B}_t . However, once we know the renegotiated liabilities \tilde{B}_t , this becomes the sufficient state for solving the model. Therefore, in the computation I will solve for the recursive equilibrium using \tilde{B}_t as a state variable.

I will use the following equilibrium conditions:

$$H_t = \phi(w_t)\tilde{B}_t, \quad (37)$$

$$\frac{B_{t+1}}{R_t^b} = \beta A_t, \quad (38)$$

$$A_t = \tilde{B}_t + (1 - w_t)H_t \quad (39)$$

$$\alpha H_t^{\frac{1}{\nu}} = w_t, \quad (40)$$

$$1 = \beta R_t^l(1 + \mu_t), \quad (41)$$

$$p_t = \beta \mathbb{E}_t \left[\chi + (1 + \eta \mu_t) p_{t+1} \right], \quad (42)$$

$$L_{t+1} = \eta \mathbb{E}_t p_{t+1}, \quad (43)$$

$$\frac{1-\tau}{\bar{R}_t^b} \geq \beta \left[1 + \frac{\theta(\omega_{t+1}) \left(\varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1} + \varphi(\omega_{t+1} - \underline{\xi}) \right)}{1 - \theta(\omega_{t+1})} \right], \quad (44)$$

$$\frac{1}{R_t^l} \geq \beta \left[1 + \theta(\omega_{t+1}) \varphi'(\omega_{t+1} - \underline{\xi}) \omega_{t+1}^2 + \theta(\omega_{t+1}) \underline{\xi} \left(\frac{1-\tau}{\beta \bar{R}_t^b} - 1 \right) \right], \quad (45)$$

$$\bar{R}_t^b = \left[1 - \theta(\omega_{t+1}) + \theta(\omega_{t+1}) \left(\frac{\underline{\xi}}{\omega_{t+1}} \right) \right] R_t^b, \quad (46)$$

$$\omega_{t+1} = \frac{B_{t+1}}{L_{t+1}} \quad (47)$$

Equations (37)-(39) come from the aggregation of the optimal policies of entrepreneurs (labor demand, savings and end of periods wealth). Equations (40)-(43) come from the optimization problem of workers (labor supply, optimal borrowing, optimal holding of the fixed asset, and borrowing constraint). Notice that the borrowing constraint of workers (equation (43) is not always binding. However, when it is not binding and the multiplier is $\mu_t = 0$, workers' borrowing is not determined. Therefore, without loss of generality I assume that in this case workers borrow up to the limit. This explains why the borrowing constraint is always satisfied with equality. Equations (44)-(45) are the first order conditions of banks. These conditions are satisfied with equality if $\omega_{t+1} < 1$ and with inequality if $\omega_{t+1} = 1$. Equation (46) defines the expected return on bank liabilities given the price of these liabilities, that is, the inverse of R_t^b . The final equation (47) simply defines leverage.

One complication in solving this system of equations is that the expectation of the next period price of the fixed asset, $\mathbb{E}_t p_{t+1}$, is unknown. All we know is that the next period price is a function of \tilde{B}_{t+1} , that is, $p_{t+1} = P(\tilde{B}_{t+1})$. If I knew the function $P(\tilde{B}_{t+1})$, for any given state \tilde{B}_t , the above conditions would be a system of 11 equations in 11 variables: $H_t, A_t, \mu_t, w_t, p_t, R_t^b, R_t^l, \bar{R}_t^b, B_{t+1}, L_{t+1}, \omega_{t+1}$. Notice that \tilde{B}_{t+1} is a known function of B_{t+1}, L_{t+1} and the realization of the sunspot shock ε . Therefore, I can compute the expectation of the next period price p_{t+1} if I know the function $P(\tilde{B}_{t+1})$. We can then solve the 11 equations for the 11 variables and this would provide a solution for any given state \tilde{B}_t .

The problem is that I do not know the function $P(\tilde{B}_{t+1})$. Therefore, the procedure will be based on a parametrization of an approximation of this function. In particular, I approximate $P(\tilde{B}_{t+1})$ with a piece-wise linear function over a grid for the state variable \tilde{B}_t . I then solve the above system of equations at each grid point for \tilde{B}_t . As part of the solution I obtain the current price p_t . I then use the

solution for the current price to update the approximated function $P(\tilde{B}_{t+1})$ at the grid point. I repeat the iteration until convergence, that is, the values guessed for $P(\tilde{B}_{t+1})$ at each grid point must be equal (up to a small rounding number) to the values of p_t obtained by solving the model (given the guess for $P(\tilde{B}_{t+1})$).

H.2 Equilibrium with structural break

When the external demand for bank liabilities changes over time or there are innovations that change the operation cost of banks, the economy transits from a stochastic equilibrium to a new stochastic equilibrium. This requires to solve for the transition and the solution method is based on the following steps.

1. I first compute the stochastic equilibrium under the regime that proceeds the structural break (the foreign demand for bank liabilities is constant at the initial level and/or the operation cost of banks is constant at the initial level).
2. I then compute the stochastic equilibrium under the terminal regime (the foreign demand of bank liabilities remains constant at the new level after the transition and/or the operation cost of banks remains constant at the new level).
3. At this point I solve the model backward at any time t starting at the terminal period when the external demand and the operation cost remain constant at the new levels. At each t I solve the system (37)-(47) using the approximated function $P_{t+1}(\tilde{B}_{t+1})$ found at time $t+1$. In the first backward step (last period of the transition), $P_{t+1}(\tilde{B}_{t+1})$ is the approximated price function found in the stochastic stationary equilibrium after the break (see previous computational step).

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